

# Unsupervised Distance Learning by Rank Correlation Measures for Image Retrieval

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## 1. Introduction

Recently, unsupervised post-processing approaches have been attracted a lot of attention in image retrieval tasks, achieving significant improvements in the effectiveness of image search systems.

For global distance analysis, the ranked lists represents a rich source of information, establishing relationships not only between pair of images (as distance measures), but among all images in a collection. In this scenario, we exploit rank correlation measures for unsupervised distance learning tasks.

In summary, the contributions of this work are threefold:

- The RL-Sim\* Algorithm, which uses information from both rank correlation measures and top-k lists overlap;
- The evaluation of six different rank correlation measures for the proposed algorithm;
- The proposal of two novel rank correlation measures for unsupervised distance learning.

## 2. RL-Sim\* Algorithm

The RL-Sim Algorithm is a recently proposed unsupervised distance learning method that improves the effectiveness of image retrieval tasks though an iterative re-ranking scheme based on rank correlation measures between top-k positions.

However, where there is no overlap between top-k positions, the rank correlation measures have no enough information for improving the distance measure.

Therefore, the RL-Sim\* considers segmented the ranked lists for computing the new distance measures.

## 3. Rank Correlation Measures

The RL-Sim and RL-Sim\* presents a generic modelling, allowing the use of different rank correlation measure. In this work, six classical and recent correlation measures were evaluated:

- Intersection Measure:** based on the overlap between top-k lists at different depths;
- Kendall  $\tau$ :** a traditional rank correlation measure, based on the number of concordant pairs in the rankings;
- Spearman:** can be seen as the L1 distance between two permutations;
- Godman:** based on the number of concordant and non-concordant pairs;
- Jaccard:** distance the Jaccard coefficient is a well-known distance between sets;
- Rank Biased Overlap (RBO):** a recently proposed rank correlation measure that compares the overlap of the two rankings at incrementally increasing depths.

**Two novel correlation measures were proposed:** Kendall  $\tau_w$  and Jaccard<sub>*l*</sub>. Both the original Kendall and Jaccard measures does not assign higher weights to top positions of ranked lists. The novel proposed measures address this drawback.

## 4. Experimental Evaluation

Extensive experiments were conducted considering four different public image collections:

- *Soccer* (280 images, 3 descriptors); *MPEG-7* (1,400 images, 6 descriptors); *Brodatz* (1,176 images, 3 descriptors); *N-S Dataset* (10,200 images, 5 descriptors).

### •RL-Sim\* Algorithm – Effectiveness Evaluation:

N-S Dataset, considering the N-S score (interval [1,4]):

Descriptor	Initial Score	Intersection	Kendall $\tau$	Spearman	Goodman	Jaccard	RBO	Jaccard <sub><i>l</i></sub>	Kendall $\tau_w$
ACC	3.36	3.54	3.51	3.45	1.06	3.47	3.54	<b>3.55</b>	3.52
BIC	3.04	3.20	3.17	3.02	1.05	3.13	3.19	<b>3.21</b>	3.19
CEED	2.61	2.75	2.71	2.56	1.04	2.68	2.75	<b>2.76</b>	2.74
FC7H	2.73	2.84	2.79	2.63	1.04	2.77	2.84	<b>2.85</b>	2.81
JCD	2.79	2.92	2.88	2.72	2.87	2.85	2.92	<b>2.93</b>	2.9
SIFT	2.54	2.81	2.82	<b>2.86</b>	1.03	2.77	2.79	2.80	2.80
<b>Average</b>	2.84	3.01	2.98	2.87	1.35	2.94	3.01	<b>3.02</b>	2.99

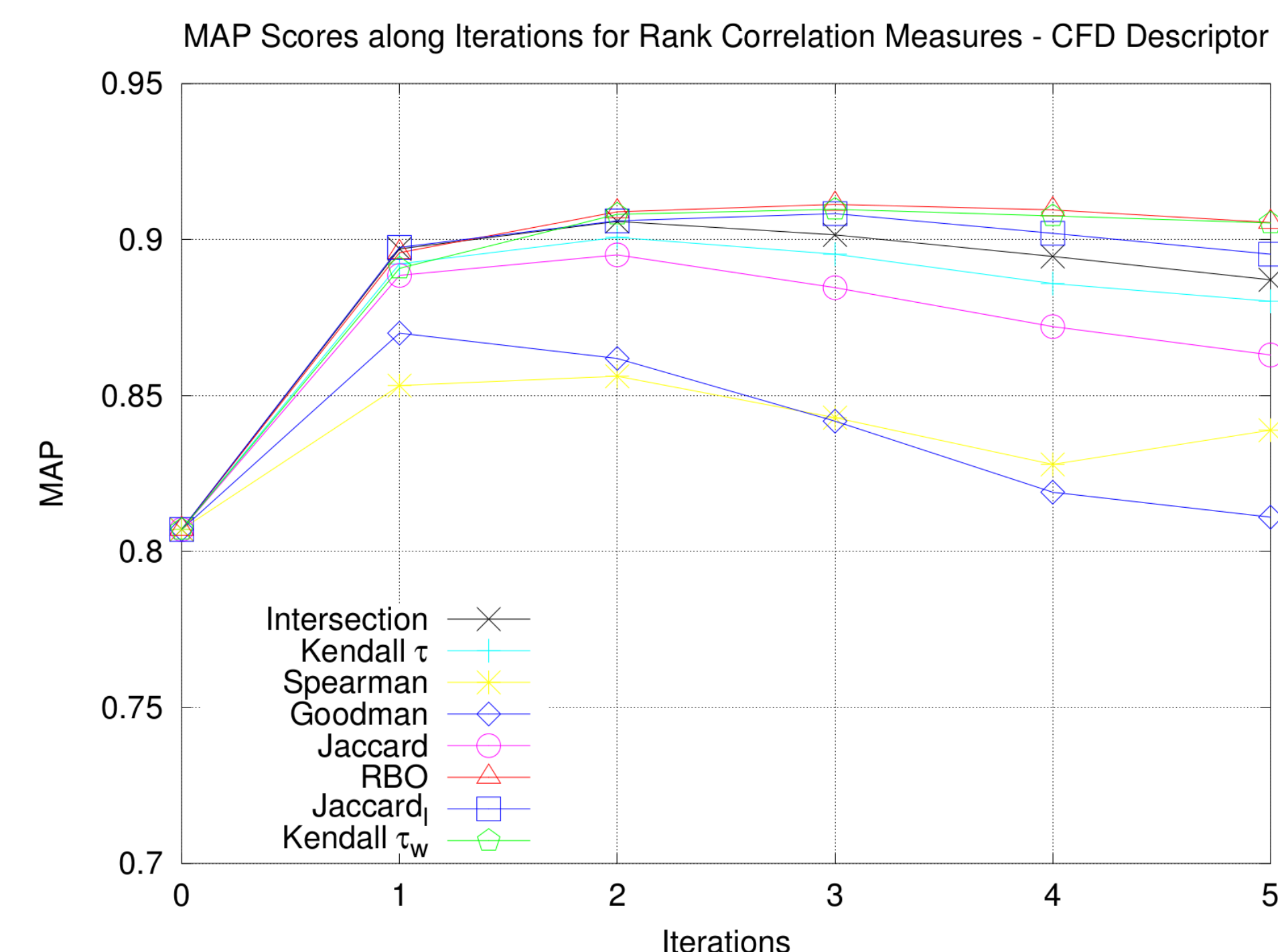
MPEG-7, Soccer and Brodatz, considering MAP as score:

Descriptor	Type	Initial MAP	Intersection	Kendall $\tau$	Spearman	Goodman	Jaccard	RBO	Jaccard <sub><i>l</i></sub>	Kendall $\tau_w$
SS	Shape	37.67	44.10	46.54	44.70	44.11	45.49	44.23	46.60	<b>47.87</b>
BAS	Shape	71.52	76.05	76.12	75.94	72.61	74.87	77.34	77.51	<b>77.75</b>
IDSC	Shape	81.70	87.38	87.59	85.03	83.50	87.03	<b>88.26</b>	88.08	88.02
CFD	Shape	80.71	90.15	90.07	86.57	86.19	89.51	<b>91.13</b>	90.91	90.81
ASC	Shape	85.28	89.96	90.14	88.03	85.75	89.54	90.57	90.77	<b>90.84</b>
AIR	Shape	89.39	96.17	95.94	<b>97.86</b>	96.08	97.72	96.08	96.78	97.23
GCH	Color	32.24	33.99	33.93	34.29	33.38	33.43	33.99	34.04	<b>34.39</b>
ACC	Color	37.23	45.19	<b>45.94</b>	44.91	42.77	45.63	44.03	44.60	45.75
BIC	Color	39.26	45.42	45.10	45.40	43.05	44.56	45.10	45.47	<b>45.50</b>
LBP	Texture	48.40	48.83	48.94	47.32	49.06	46.53	<b>51.00</b>	50.10	49.92
CCOM	Texture	57.57	62.89	62.44	59.02	61.19	61.37	<b>64.23</b>	64.06	63.53
LAS	Texture	75.15	78.58	78.49	75.74	75.76	76.76	<b>79.80</b>	79.57	79.34
<b>Average</b>	-	61.34	66.56	66.77	65.4	59.93	66.04	67.15	67.37	<b>67.59</b>

- Summary of Best MAP scores for MPEG-7, Soccer and Brodatz datasets:

Descriptor	Initial MAP	Rank Measure	RL-Sim* MAP	Relative Gain (%)
SS	37.67	Kendall $\tau_w$	47.87	+27.08
BAS	71.52	Kendall $\tau_w$	77.75	+8.71
IDSC	81.70	RBO	88.26	+8.03
CFD	80.71	RBO	91.13	+12.91
ASC	85.28	Kendall $\tau_w$	90.84	+6.52
AIR	89.39	Spearman	97.86	+9.48
GCH	32.24	Kendall $\tau_w$	34.39	+6.67
ACC	37.23	Kendall $\tau$	45.94	+23.40
BIC	39.26	Kendall $\tau_w$	45.50	+15.89
LBP	48.40	RBO	51.00	+5.37
CCOM	57.57	RBO	64.23	+11.57
LAS	75.15	RBO	79.80	+6.19

### •Impact of parameter k for different measures (MPEG-7 dataset):



### •Correlation among Rank Correlation Measures:

Rank Measures	(I)	(K)	(S)	(G)	(J)	(R)	(J <sub><i>l</i></sub> )	(K <sub><i>w</i></sub> )
(I) Intersection	1	0.23	0.31	0.74	0.77	0.65	0.65	0.31
(K) Kendall $\tau$	0.23	1	0.75	0.22	0.55	0.61	0.63	0.98
(S) Spearman	0.31	0.75	1	0.19	0.52	0.47	0.65	0.76
(G) Goodman	0.74	0.22	0.19	1	0.82	0.86	0.86	0.28
(J) Jaccard	0.77	0.55	0.52	0.82	1	0.86	0.91	0.55
(R) RBO	0.65	0.61	0.47	0.86	0.86	1	0.99	0.65
(J <sub><i>l</i></sub> ) Jaccard <sub><i>l</i></sub>	0.65	0.63	0.49	0.86	0.91	0.99	1	0.66
(K <sub><i>w</i></sub> ) Kendall $\tau_w$	0.31	0.98	0.76	0.28	0.55	0.65	0.66	1

## 5. Conclusions

In this work, we have presented an unsupervised distance learning approach based on rank correlation measures: the the RL-Sim\* Algorithm, which considers the rank correlation measures and the overlap between the neighborhood sets aiming at computing a more effective distance measure.

Six traditional measures were evaluated and two novel rank correlation measures were proposed specially for the unsupervised distance learning problem on image retrieval tasks.

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