

# Region-based Image Representation

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- Superpixel segmentation should represent objects by the union of their superpixels.
- The methods may be non-hierarchical and hierarchical, being the latter divided into sparse or dense hierarchies [1].
- This lecture presents a recent non-hierarchical graph-based approach [2], named Dynamic Iterative Spanning Forest (DISF), and discusses its extension to hierarchical segmentation.

# Agenda

- Seed-based superpixel segmentation: the traditional pipeline.
- The DISF pipeline and its motivation.
- The DISF algorithm.
- How to extend it to hierarchical segmentation.

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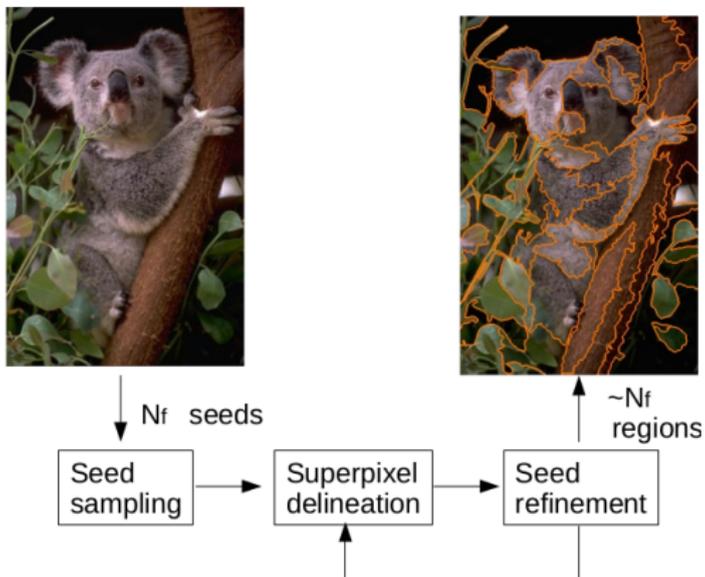
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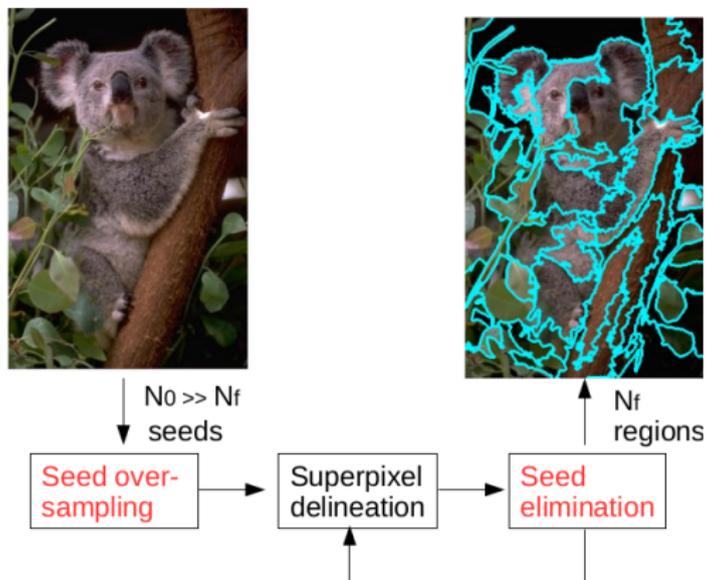
They usually do not guarantee the desired number of superpixels and the algorithm for superpixel delineation plays the main role.

# Seed-based superpixel segmentation



The Iterative Spanning Forest (ISF) approach [3], for example, relies on the Image Foresting Transform (IFT) algorithm [4] for superpixel delineation.

# The DISF pipeline



DISF starts from a much higher number  $N_0$  of seeds, also uses the IFT algorithm for superpixel delineation, and eliminates the number of seeds until the desired number  $N_f$ .

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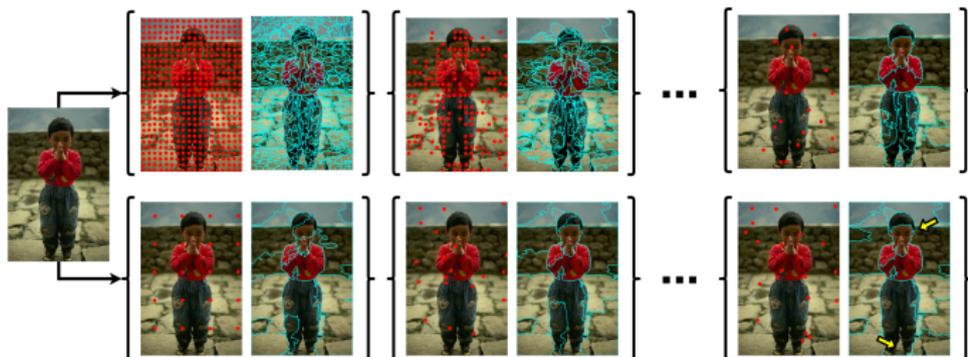
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- It uses a connectivity function in the IFT algorithm that guarantees an **optimum-path forest** – each superpixel is an optimum-path tree rooted at its seed.
- One can apply **application-dependent criteria** to retain relevant seeds at each iteration.
- It improves superpixel delineation for **lower numbers of superpixels**.

# Motivation for DISF



DISF (above) versus ISF (below) for lower number of superpixels.  
(Figure from [2].)

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# The DISF algorithm

- DISF uses **grid sampling** – a uniform seed distribution – to start the process.
- The IFT algorithm estimates arc-weights dynamically for the max-arc-weight function  $f_{\max}$  based on image properties of the growing trees [5, 6] – this improves **boundary adherence**.
- Seed elimination is based on **mid-level image properties** of the resulting superpixel graph – it can better identify irrelevant superpixels for seed elimination and their relevant borders can be recovered in the next iteration.

# The IFT algorithm for dynamic trees

Let  $(D_I, \mathcal{A}, \mathbf{I})$  be an image graph and  $\mathcal{S} = \mathcal{S}_0$  be the initial seed set with  $N_0$  samples.

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DISF uses the version of  $f_{\max}$  below as path-cost function:

$$\begin{aligned}f_{\max}(\langle q \rangle) &= \begin{cases} 0 & \text{if } q \in \mathcal{S}, \\ +\infty & \text{otherwise.} \end{cases} \\f_{\max}(\pi_p \cdot \langle p, q \rangle) &= \max\{f_{\max}(\pi_p), \|\mu_{\mathcal{T}_{R(p)}} - \mathbf{I}(q)\|_2\}, \\ \mu_{\mathcal{T}_{R(p)}} &= \frac{1}{|\mathcal{T}_{R(p)}|} \sum_{q \in \mathcal{T}_{R(p)}} \mathbf{I}(q),\end{aligned}$$

where  $\mathcal{T}_{R(p)}$  is the growing tree that contains  $p$  and rooted  $R(p) \in \mathcal{S}$ .

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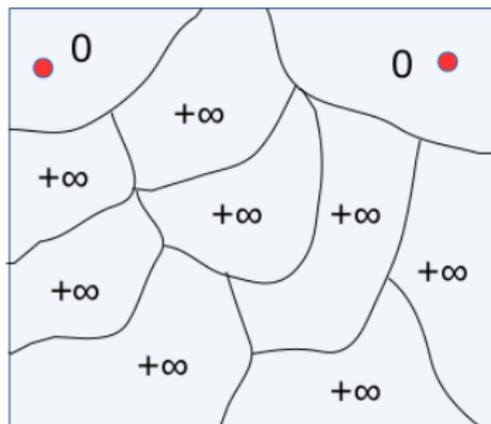
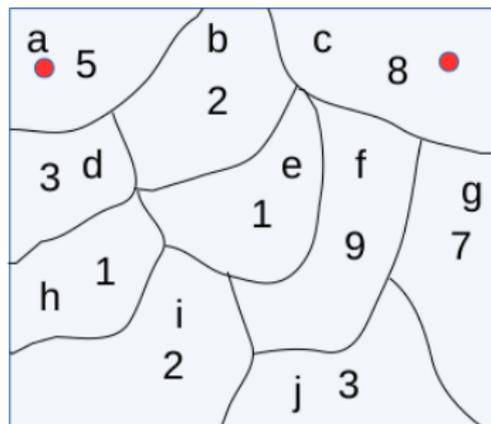
We call it segmentation by **dynamic trees** and other variants can be found in [5, 6].

# The IFT algorithm for dynamic trees

- 1 For each  $q \in D_I$ , do
- 2 Set  $V(q) \leftarrow +\infty$ ,  $R(q) \leftarrow q$ , and  $P(q) \leftarrow nil$ .
- 3 If  $q \in \mathcal{S}$  then  $V(q) \leftarrow 0$ .
- 4 Set  $S_{\tau_q} \leftarrow 0$ ,  $N_{\tau_q} \leftarrow 0$ , and insert  $q$  in  $Q$ .
- 5 While  $Q \neq \emptyset$  do
- 6 Remove from  $Q$  the node  $p = \arg \min_{q \in Q} \{V(q)\}$ .
- 7 Set  $S_{\tau_{R(p)}} \leftarrow S_{\tau_{R(p)}} + \frac{I(p) - S_{\tau_{R(p)}}}{N_{\tau_{R(p)}} + 1}$  and  $N_{\tau_{R(p)}} \leftarrow N_{\tau_{R(p)}} + 1$ .
- 8 Set  $\mu_{\tau_{R(p)}} \leftarrow \frac{S_{\tau_{R(p)}}}{N_{\tau_{R(p)}}}$ .
- 9 For each  $q \in \mathcal{A}(p)$ ,  $q \in Q$ , do
- 10 If  $V(q) > \max\{V(p), \|\mu_{\tau_{R(p)}} - \mathbf{I}(q)\|_2\}$ , then
- 11 Set  $V(q) \leftarrow \max\{V(p), \|\mu_{\tau_{R(p)}} - \mathbf{I}(q)\|_2\}$ ,
- 12  $R(q) \leftarrow R(p)$ , and  $P(q) \leftarrow p$ .

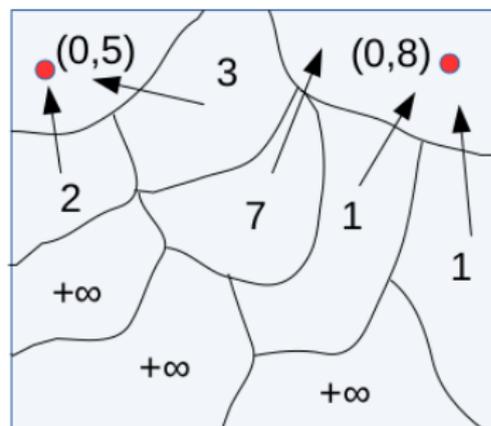
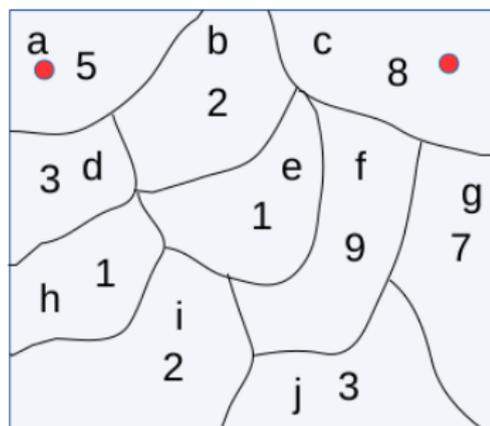
# Example

This example applies dynamic trees on an implicit **region adjacency graph** whose letters indicate nodes and numbers indicate node intensity on the left.



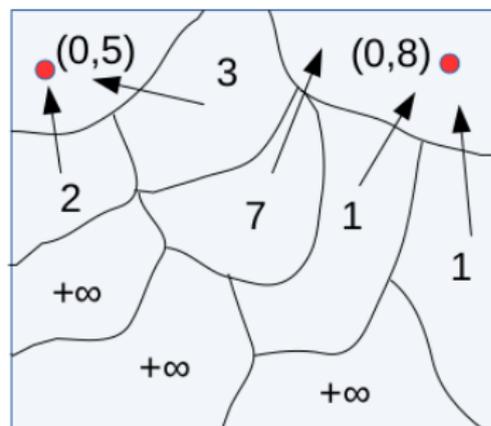
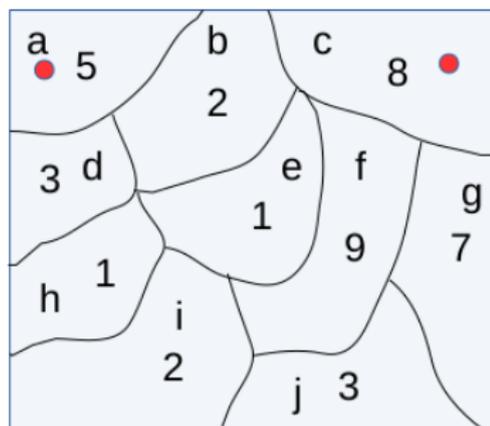
Trivial trees with initial costs on the right, forced to be zero on two root nodes, a and c (red).

# Example



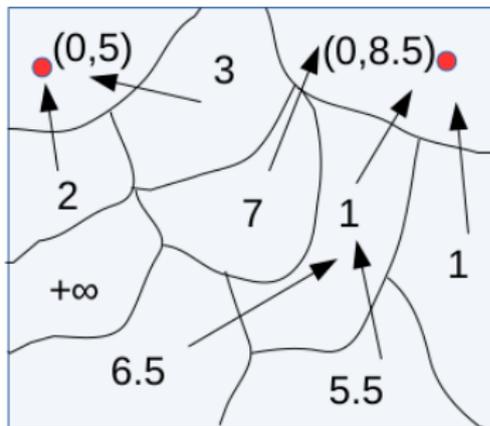
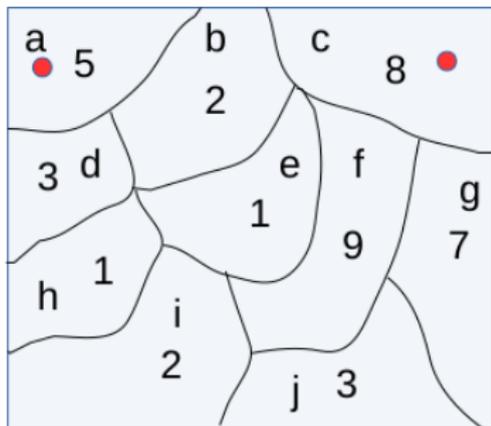
- After two IFT iterations on the right, when  $a$  and  $c$  are removed from  $Q$ , and **path costs** (numbers) and **predecessors** (arrows) of its adjacent nodes change.

# Example



- After two IFT iterations on the right, when  $a$  and  $c$  are removed from  $Q$ , and **path costs** (numbers) and **predecessors** (arrows) of its adjacent nodes change.
- The notation  $(x, y)$  indicates cost  $V(r) = x$  and mean  $\mu_{\tau_r} = y$  for nodes in the **growing tree**  $\tau_r$  rooted on node  $r$ .

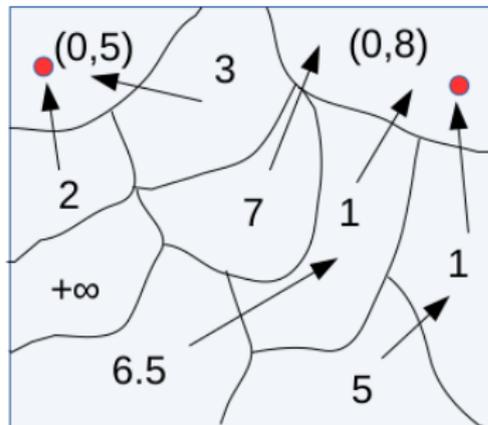
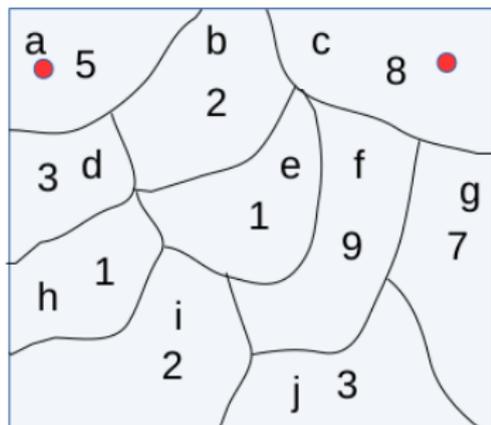
# Example



- When  $f$  is removed from  $Q$  (right, third IFT iteration), the mean  $\mu_{TR(f)}$  changes to  $\frac{I(c)+I(f)}{2} = 8.5$ .

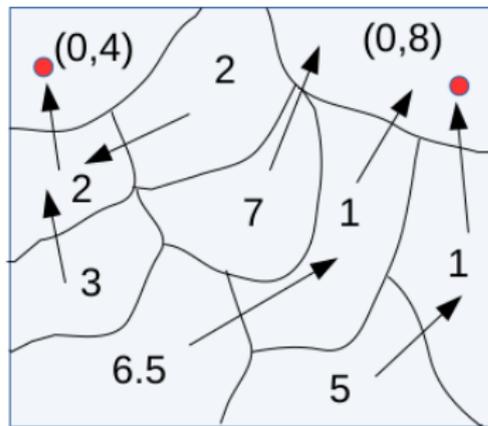
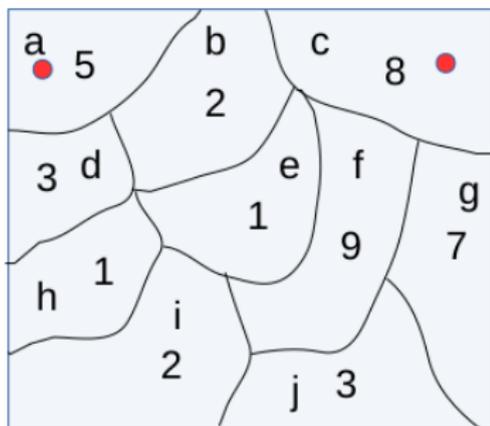


# Example



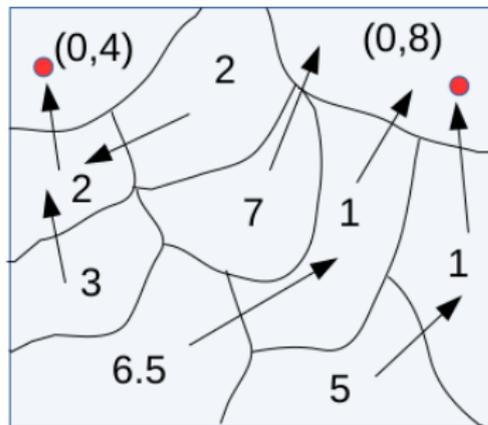
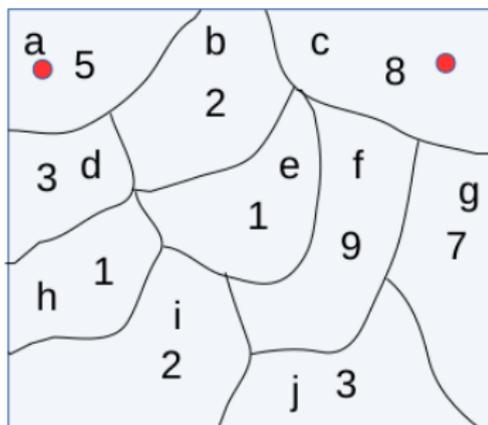
When  $g$  is removed from  $Q$  (right, fourth IFT iteration), the mean  $\mu_{\mathcal{T}_{R(g)}}$  changes to  $\frac{I(c)+I(f)+I(g)}{3} = 8$  and it conquers  $j$  with cost 5.

# Example



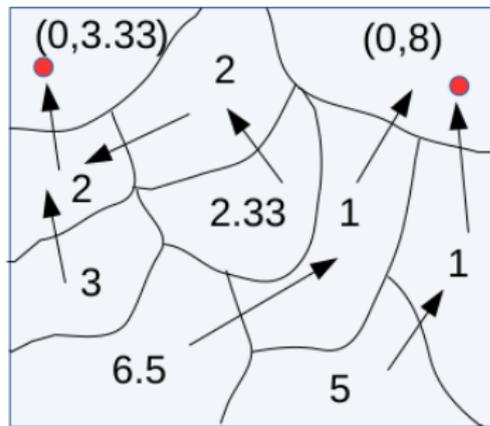
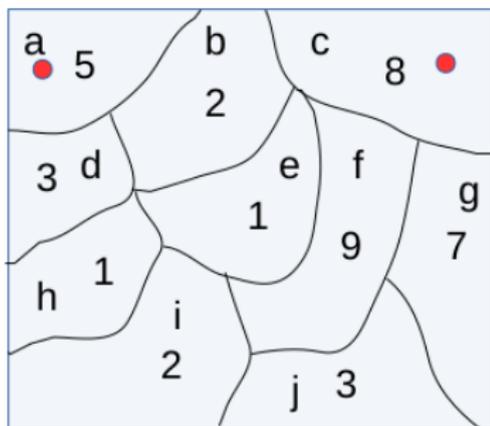
- When  $d$  is removed from  $Q$  (right, fifth IFT iteration), the mean  $\mu_{\mathcal{T}_{R(d)}}$  changes to  $\frac{I(a)+I(d)}{2} = 4$ .

# Example



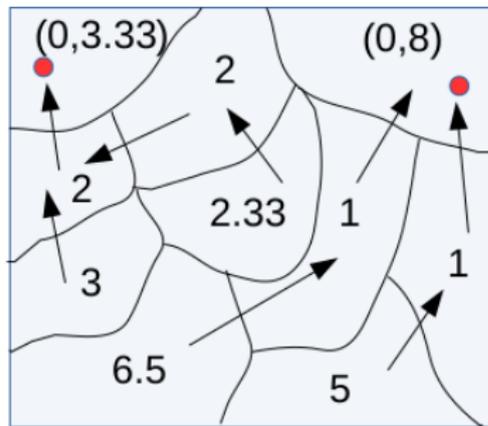
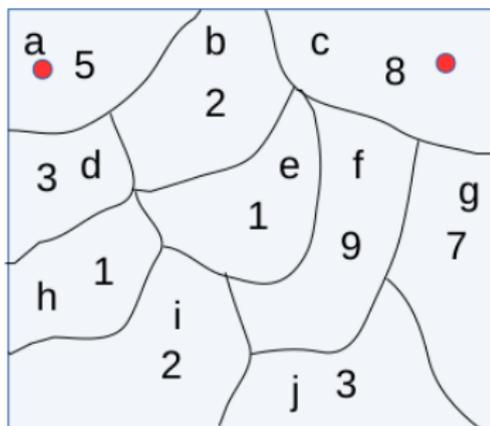
- When  $d$  is removed from  $Q$  (right, fifth IFT iteration), the mean  $\mu_{\tau_{R(d)}}$  changes to  $\frac{I(a)+I(d)}{2} = 4$ .
- It conquers  $b$  and  $h$  by changing predecessors and costs to  $P(b) = d$ ,  $V(b) = 2$ ,  $P(h) = d$ , and  $V(h) = 3$ .

# Example



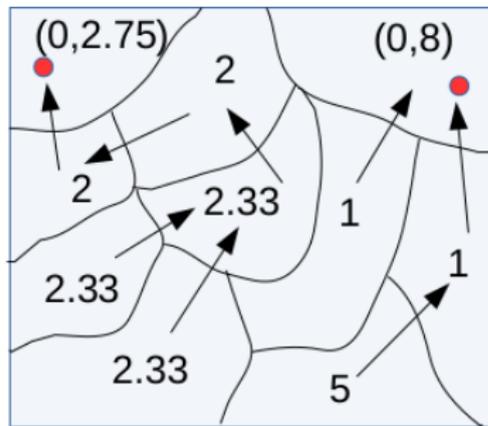
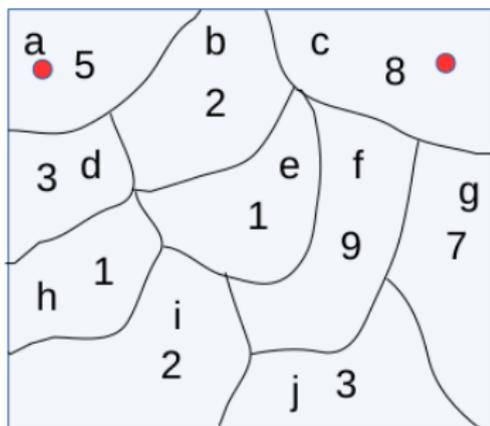
- When  $b$  is removed from  $Q$  (right, sixth IFT iteration), the mean  $\mu_{\mathcal{T}_{R(b)}}$  changes to  $\frac{I(a)+I(d)+I(b)}{3} = 3.33$ .

# Example



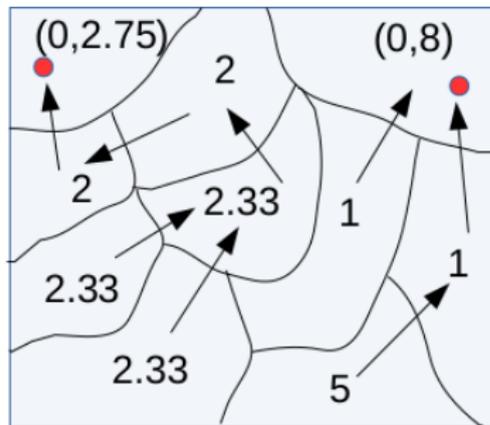
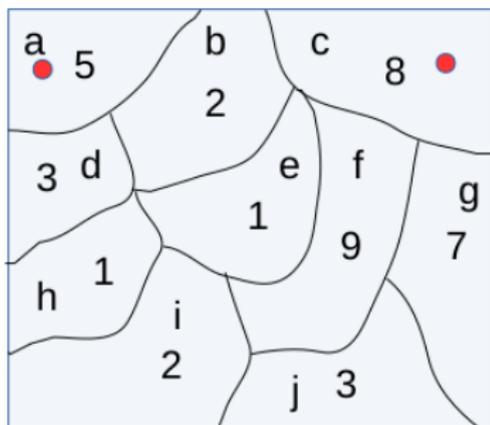
- When  $b$  is removed from  $Q$  (right, sixth IFT iteration), the mean  $\mu_{\tau_{R(b)}}$  changes to  $\frac{I(a)+I(d)+I(b)}{3} = 3.33$ .
- It conquers  $e$  by changing predecessor and cost to  $P(e) = b$  and  $V(e) = 2.33$ .

# Example



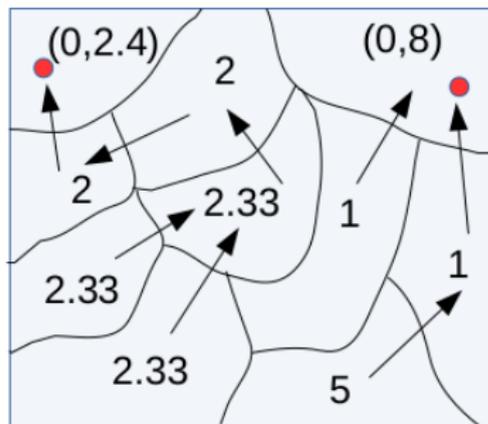
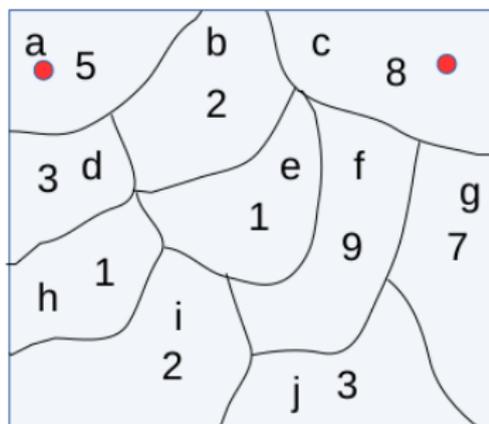
- When e is removed from  $Q$  (right, seventh IFT iteration), the mean  $\mu_{\mathcal{T}_{R(e)}}$  changes to  $\frac{I(a)+I(d)+I(b)+I(e)}{4} = 2.75$ .

# Example



- When  $e$  is removed from  $Q$  (right, seventh IFT iteration), the mean  $\mu_{\mathcal{T}_{R(e)}}$  changes to  $\frac{I(a)+I(d)+I(b)+I(e)}{4} = 2.75$ .
- It conquers  $h$  and  $i$  by changing predecessors and costs to  $P(h) = e$ ,  $V(h) = 2.33$ ,  $P(i) = e$ , and  $V(i) = 2.33$ .

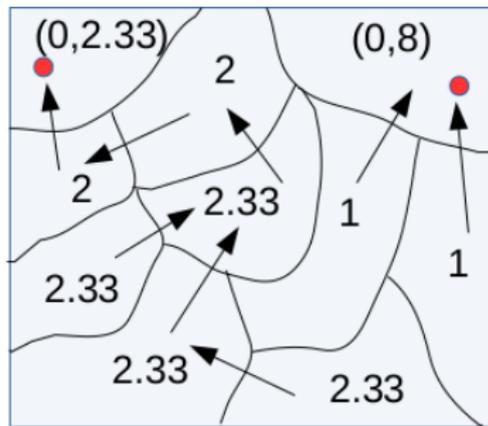
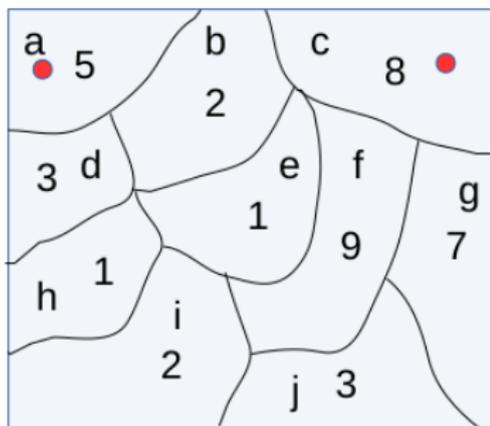
# Example



When  $h$  is removed from  $Q$  (right, eighth IFT iteration), it cannot conquer any node but the mean  $\mu_{\mathcal{T}_{R(h)}}$  changes to

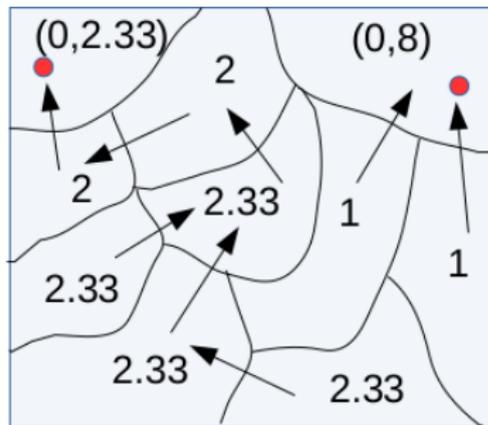
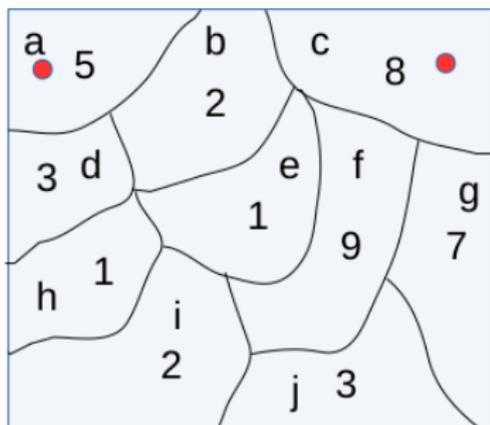
$$\frac{I(a)+I(d)+I(b)+I(e)+I(h)}{5} = 2.4.$$

# Example



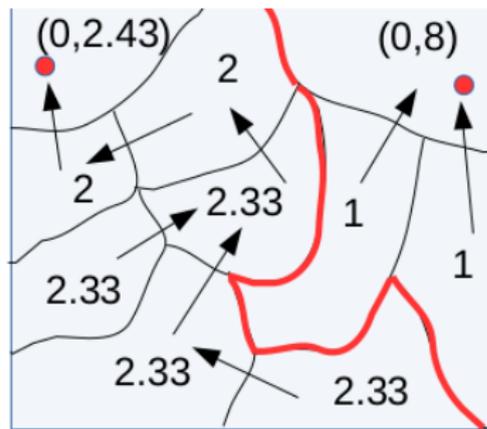
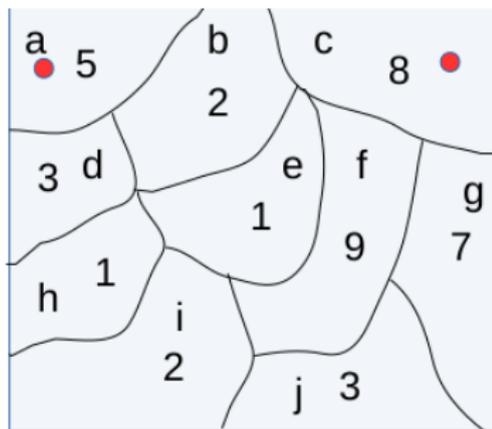
- When  $i$  is removed from  $Q$  (right, ninth IFT iteration), the mean  $\mu_{\mathcal{T}_{R(i)}}$  changes to  $\frac{I(a)+I(d)+I(b)+I(e)+I(h)+I(j)}{6} = 2.33$ .

# Example



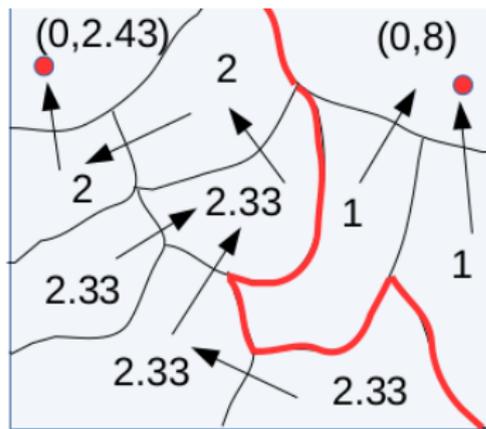
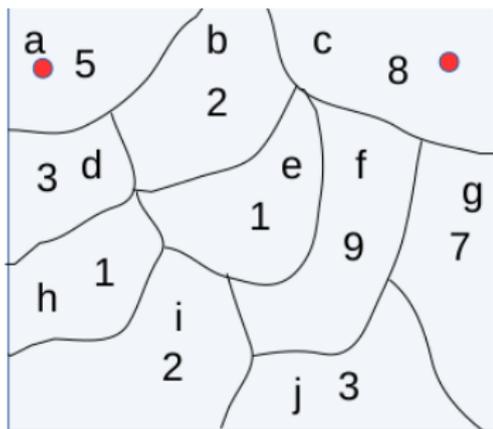
- When  $i$  is removed from  $Q$  (right, ninth IFT iteration), the mean  $\mu_{\mathcal{T}_{R(i)}}$  changes to  $\frac{I(a)+I(d)+I(b)+I(e)+I(h)+I(i)}{6} = 2.33$ .
- It conquers  $j$  by changing predecessor and cost to  $P(j) = i$  and  $V(j) = 2.33$ .

# Example



- When  $j$  is removed from  $Q$  (right, tenth IFT iteration), the mean  $\mu_{TR(j)}$  changes to  $\frac{I(a)+I(d)+I(b)+I(e)+I(h)+I(i)+I(j)}{7} = 2.43$ .

# Example



- When  $j$  is removed from  $Q$  (right, tenth IFT iteration), the mean  $\mu_{TR(j)}$  changes to  $\frac{l(a)+l(d)+l(b)+l(e)+l(h)+l(i)+l(j)}{7} = 2.43$ .
- The process terminates with two optimum path trees.

# The DISF algorithm

For a desired number  $N_f$  of superpixels.

- 1 Use grid sampling to get  $\mathcal{S}$  with  $|\mathcal{S}| = N_0 \gg N_f$  seeds.
- 2 Do
- 3   Compute  $(P, R, V) \leftarrow \text{IFT-Algorithm}(D_I, \mathbf{I}, \mathcal{A}, \mathcal{S})$ .
- 4   Update  $\mathcal{S}$  by eliminating seeds from irrelevant superpixels.
- 5 While  $|\mathcal{S}| \neq N_f$ .
- 6   Set  $i \leftarrow 1$
- 7   For each  $p \in D_I$  do
- 8     If  $R(p) = p$  then set  $L(p) \leftarrow i$  and  $i \leftarrow i + 1$ .
- 9   For each  $p \in D_I$  do
- 10    Set  $L(p) \leftarrow L(R(p))$ .
- 11 Return segmentation in the label map  $L$ .

# Seed elimination

The seed set  $\mathcal{S}_j$  for a given iteration  $j$  of loop 2-5 is defined by the  $M_j = \max\{N_0 \exp^{-j}, N_f\}$  seeds from the previous set  $\mathcal{S}_{j-1}$  with the highest values  $v(s)$ , such that

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$$v(s) = \frac{|\tau_s|}{|D_I|} \min_{(\tau_s, \tau_t) \in \mathcal{B}} \{\|\mu_{\tau_t} - \mu_{\tau_s}\|_2\}$$

is the relevance of a superpixel rooted at seed  $s \in \mathcal{S}_{j-1}$ ,

$$\mathcal{B} = \{(\tau_s, \tau_t) \in \mathcal{T} \times \mathcal{T} \mid \exists(p, q) \in \mathcal{A}, p \in \tau_s, q \in \tau_t, s \neq t\}$$

is a tree-adjacency relation, and  $\mathcal{T}$  is the set of optimum-path trees generated by the IFT algorithm.

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- Each RAG can be created from the root map  $R$ , by inserting a step between Lines 3 and 4.
- By that, the subsequent RAGs compose a **hierarchical segmentation** – a tree of connected regions where each node contains the regions of the previous segmentation.
- How does it compare with the original DISF algorithm and the recursive ISF algorithm in [1]?

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The role of optimum connectivity in image segmentation: Can the algorithm learn object information during the process?

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